\$16.? Surface Integrals
 Last time: SS FCx,y,z) ds = Sff(xum) yunging \$\six \su\ aA
Son domain D
Ex Compute $\int \int x^2 ds$ for S the surface of the unit sphere centered at the Origin
Soli We peremeterize S via derivet from spherice from Coords
$S(\theta, \theta) = \langle Sin(\theta)(os(\theta), Sin(\theta)Sin(\theta), Cos(\theta) \rangle$ on $(\theta, \theta) \in [0, 2\pi] \times [0, \pi]$
$\vec{S}_{\theta} = (-5h(4)sn(6), sin(4)cos(6), 07$ $\vec{S}_{\theta} = (cos(4)cos(6), cos(4)sin(6), -sin(4))$
Sex Sq = C J k -sn(4)sin(8) sh(4)x48 D
(0x(4)(0x(0) (0x(4)(0x(0) -51)(4)
= (-Sin?(4) cos(0), - (Sin²(4)S, (0)), - Sin 4 cos 45in²6- Sh(4) cos(4)
=-Sin (4) (Sin(4) coste), Sin(4) sin(6), (os (4)) 1 So × Su = Sin (4) Sin(4) coste) + sin(4) sin(6) + cos(4)
= Sin (φ) = Sin (φ)

1 1 1 1 1 Nev . . .

- 2

11 SS x2ds = S S12(4)(03(6) · S12(4) d9d0 Fubini's = [(03(6) da . [517 5103(4) dq. = = 1 (1+cos(20))d0 · (351(0)(1-cos(0))d9 u= cos(1) du=-sn(40)d4 = = = [0 + 2 sin(20)] (T - (1-u2) du = = = (211-0) . (-[u-4/3]) = - ++ (=(-1-==(-1))=(1-==)) = 197 WANT: A theory of suffice integrals of vector fields ... First ve need to understand what "purntation" Showle men for surfaces (changing orientation register integrals) Orientection = choice of direction I orientation should be controlled by the pormal vector) of the tengant Ino to the surface at a given point Sux5, should point "at" or "up" for positive orientection





